

# **Non-trivial effects of time-dependent level populations in SNe II atmospheres**

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Blinnikov S. I.  
Dolgov A. D.

# Main idea

## STELLA

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Hydrodynamics

Thermodynamics

Continuum

# Main idea

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LTE



Hydrodynamics

Thermodynamics

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# Main idea

STELLA

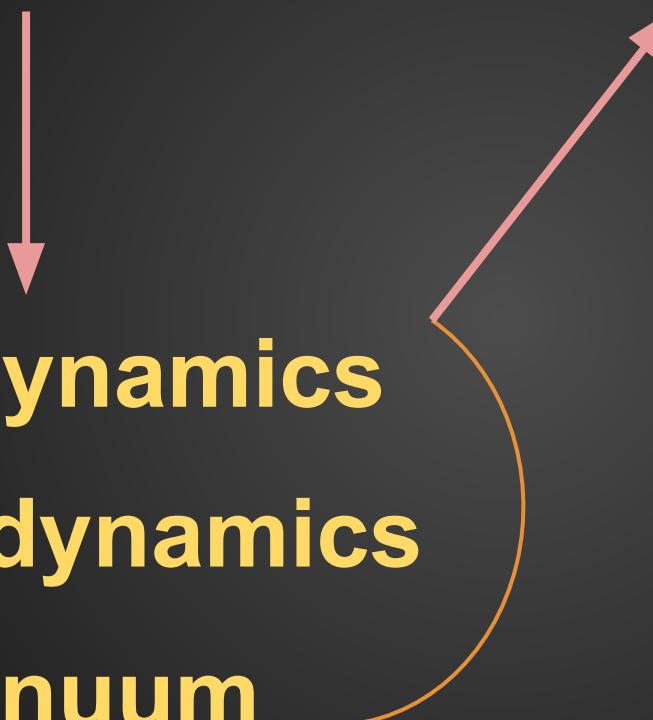
LTE

LEVELS

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STELLA

LTE

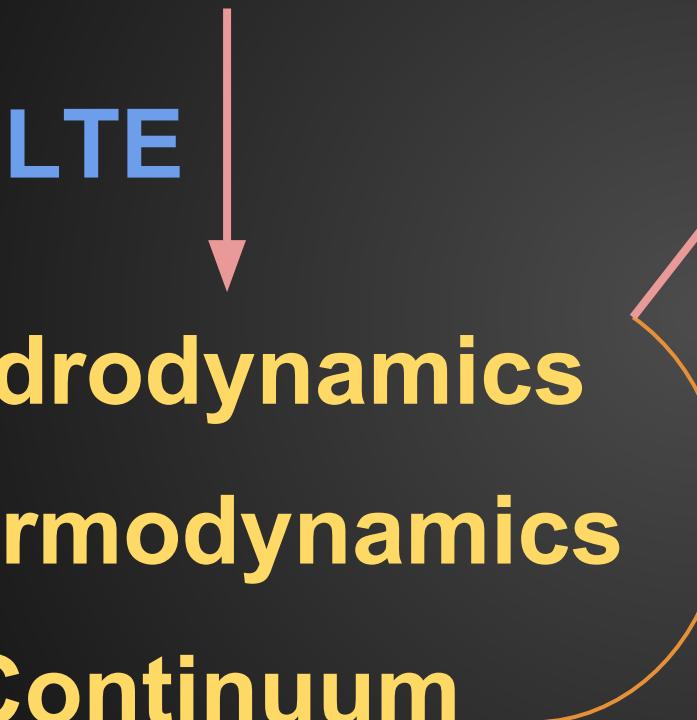
LEVELS

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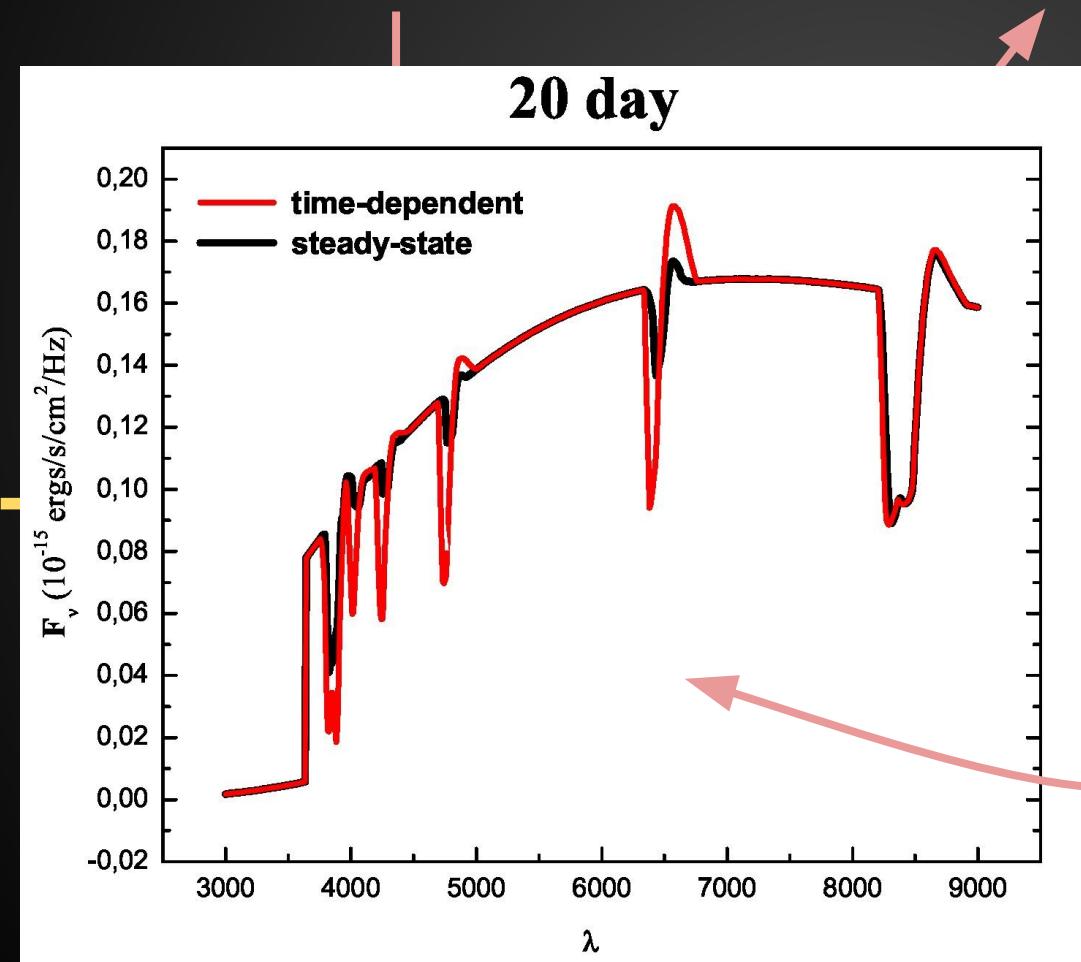
Rate equations  
Line Transfer  
Sobolev appr.



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Rate equations  
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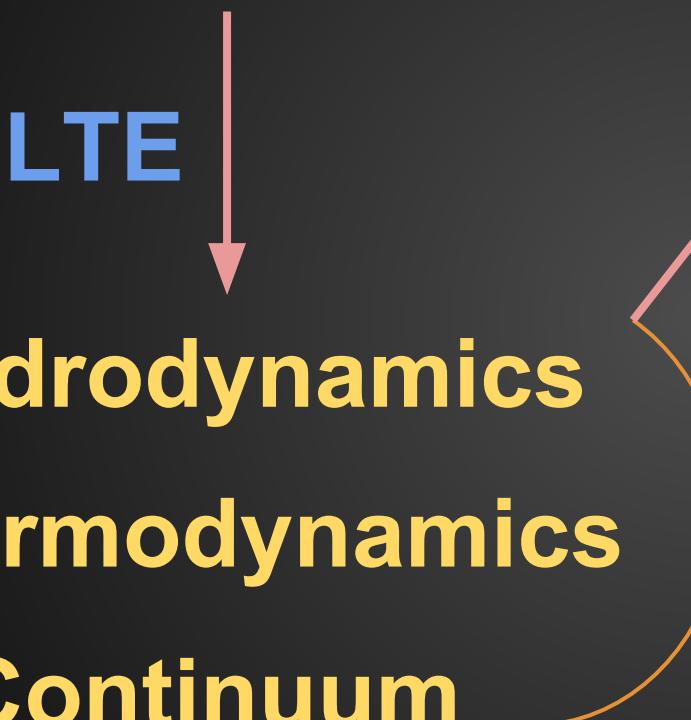
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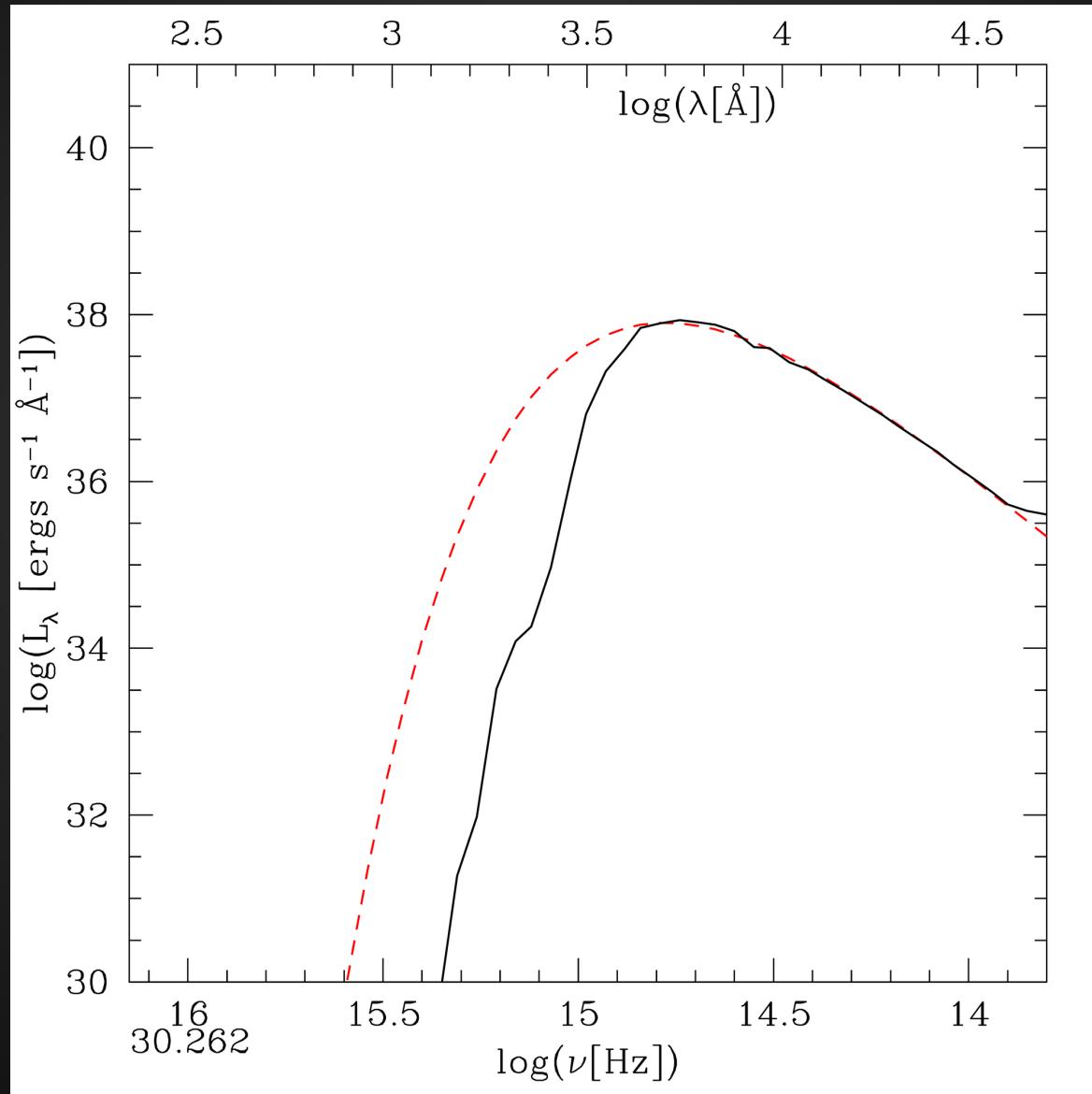
Thermodynamics

Continuum

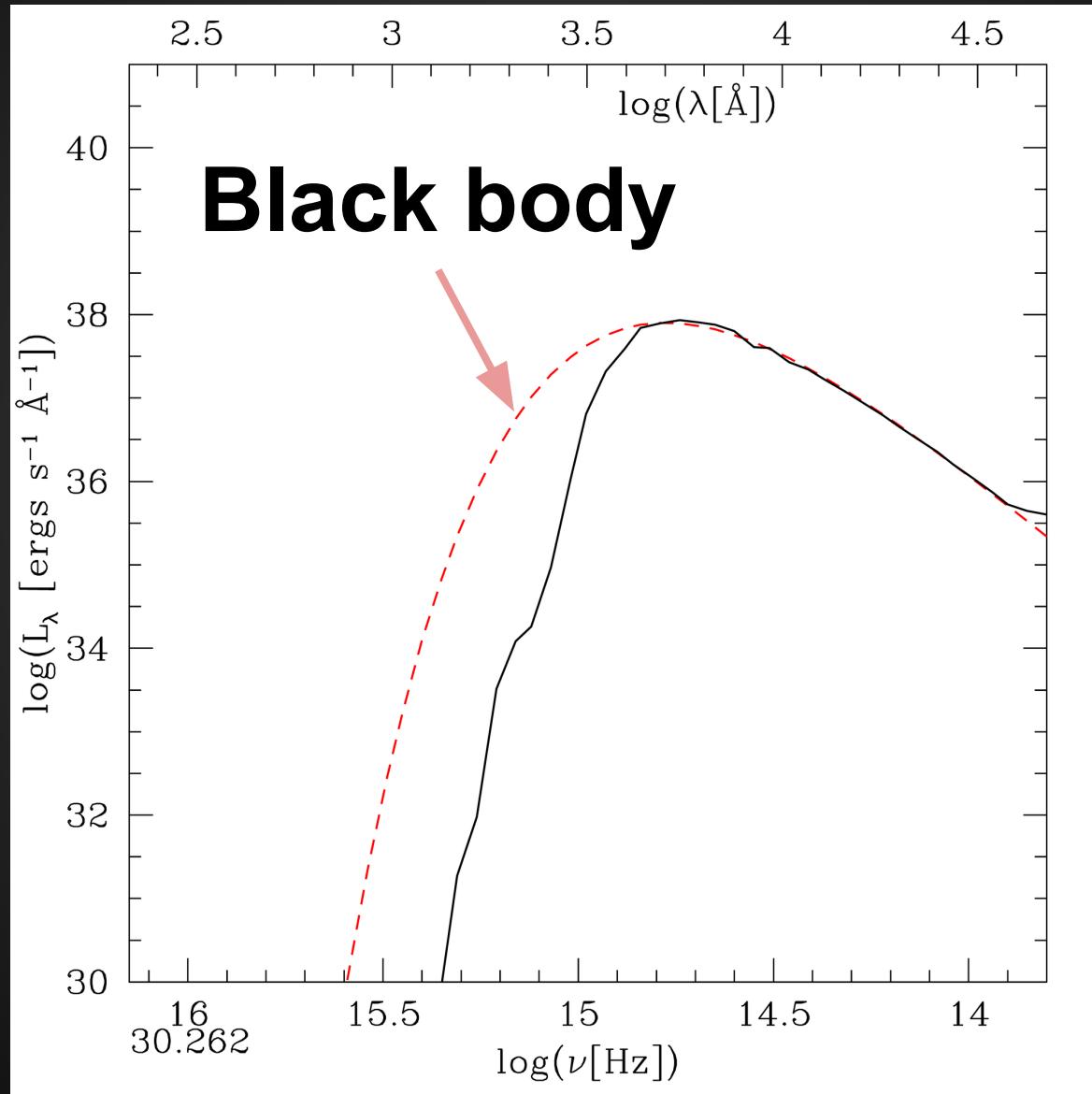
no self-consistent continuum!



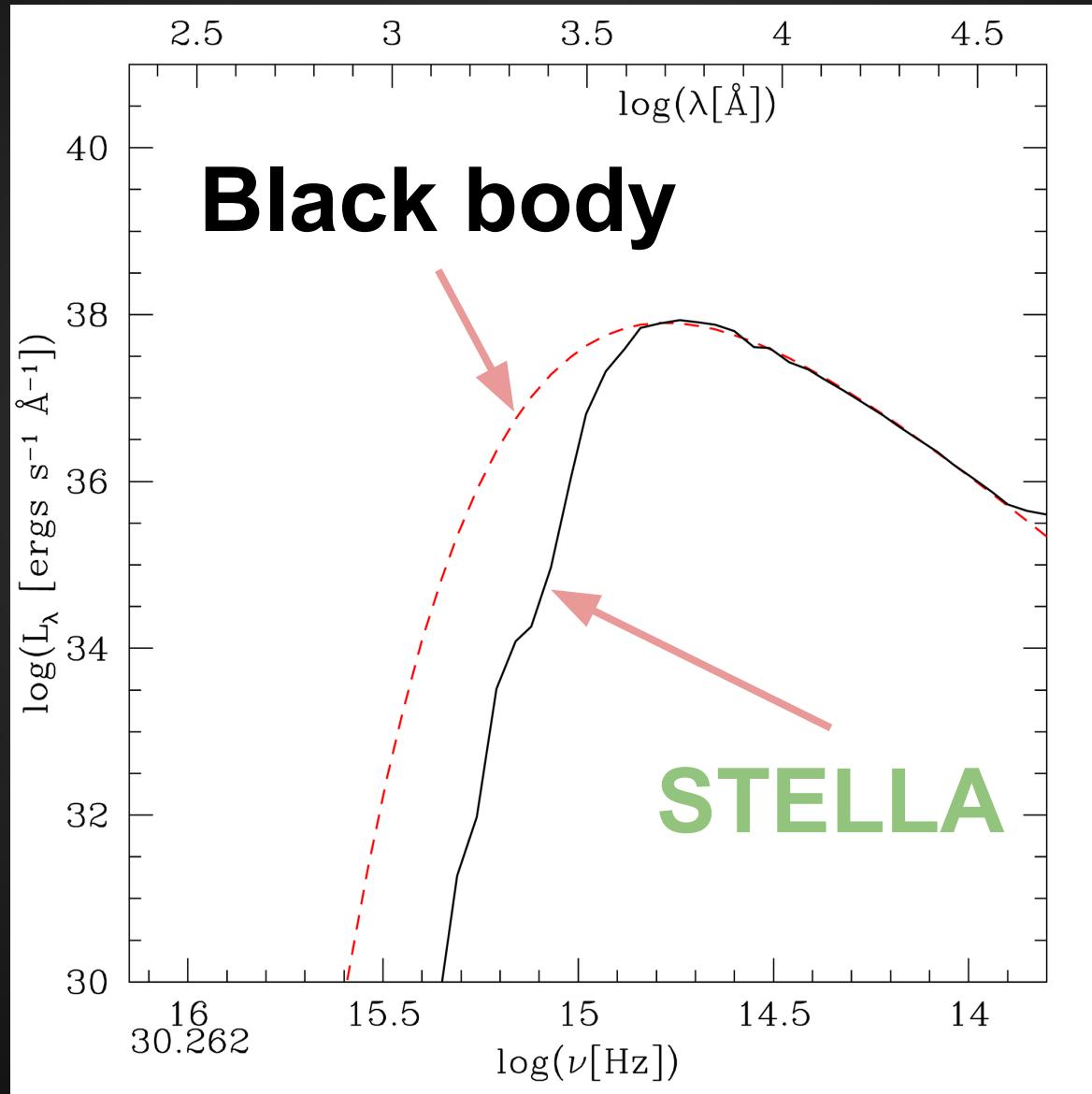
# Continuum radiation



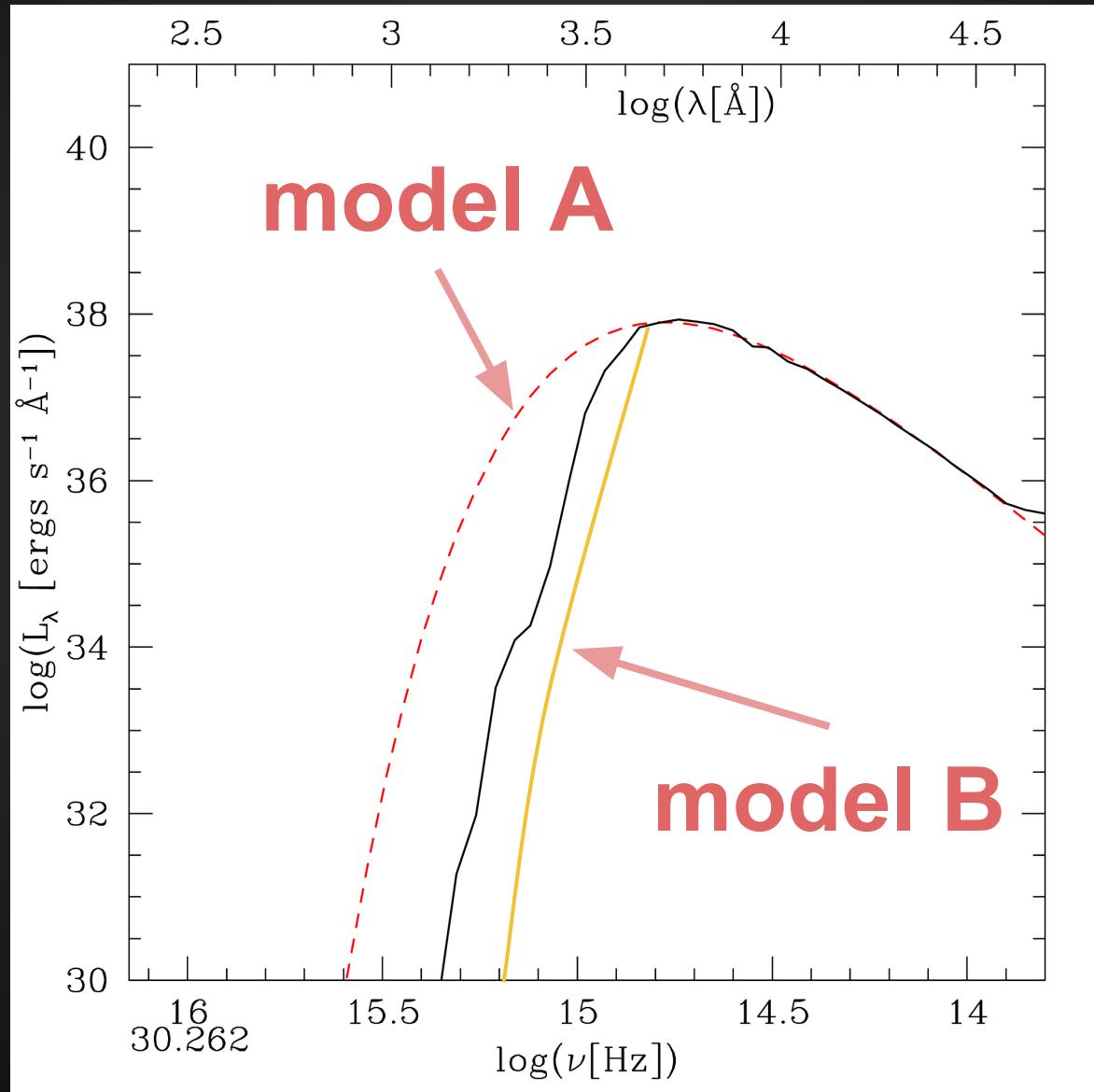
# Continuum radiation



# Continuum radiation



# Continuum radiation



# Rate equations

$$\frac{\partial n_{z,i}}{\partial t} + \operatorname{div}(n_{z,i} \vec{v}) = \sum_{j \neq i} (n_{z,j} P_{j,i} - n_{z,i} P_{i,j})$$

# Rate equations

$$\frac{\partial n_{z,i}}{\partial t} + \operatorname{div}(n_{z,i} \vec{v}) = \sum_{j \neq i} (n_{z,j} P_{j,i} - n_{z,i} P_{i,j})$$

**time-dependent**

$$\frac{D n_{z,i}}{D t} + \frac{3 n_{z,i}}{t} = \sum_{j \neq i} (n_{z,j} P_{j,i} - n_{z,i} P_{i,j})$$

# Rate equations

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time-dependent

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# Rate equations

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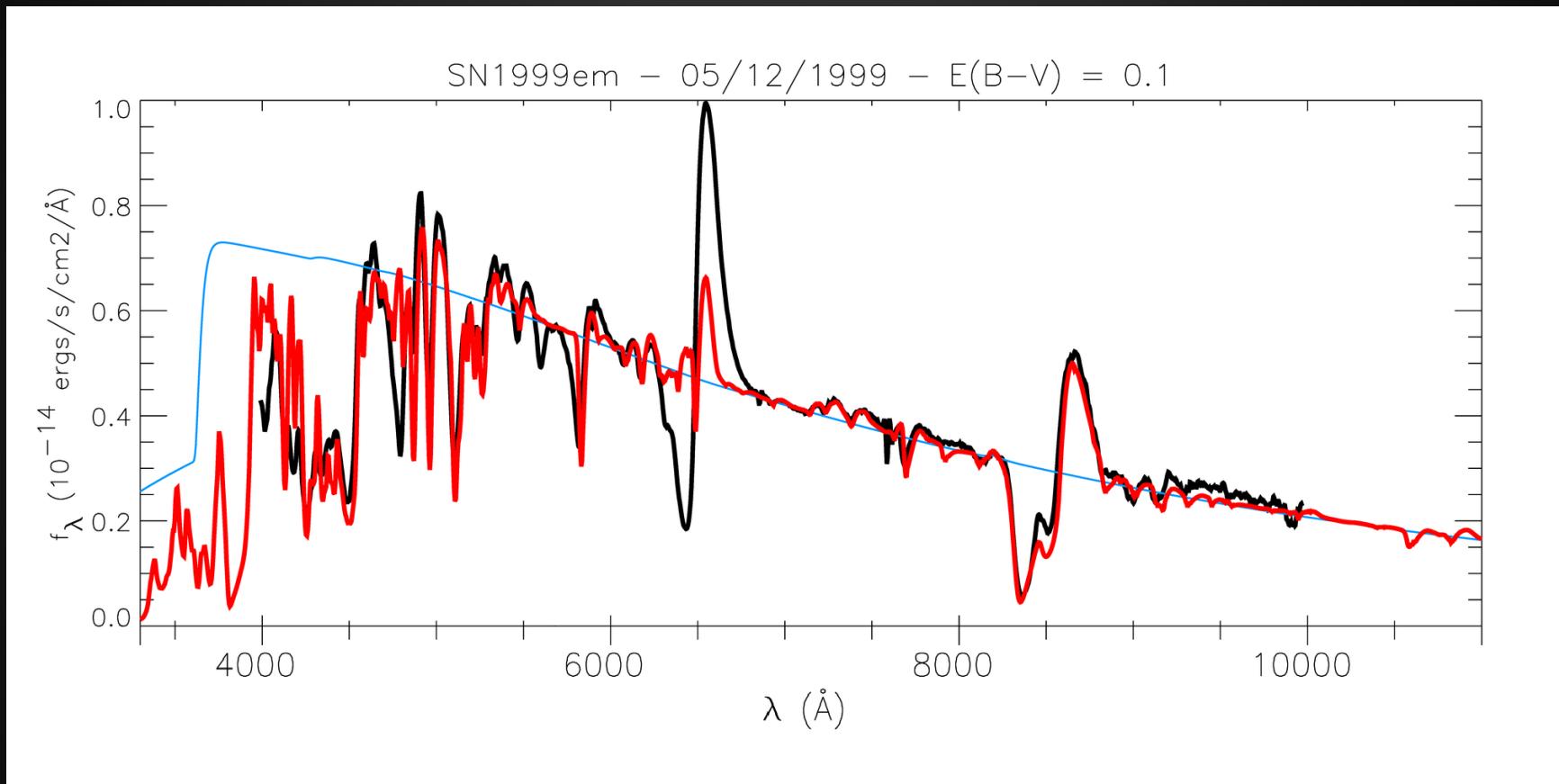
**time-dependent**

$$\cancel{\frac{Dn_{z,i}}{Dt} + \frac{3n_{z,i}}{t}} = \sum_{j \neq i} (n_{z,j} P_{j,i} - n_{z,i} P_{i,j})$$

**steady-state approximation**

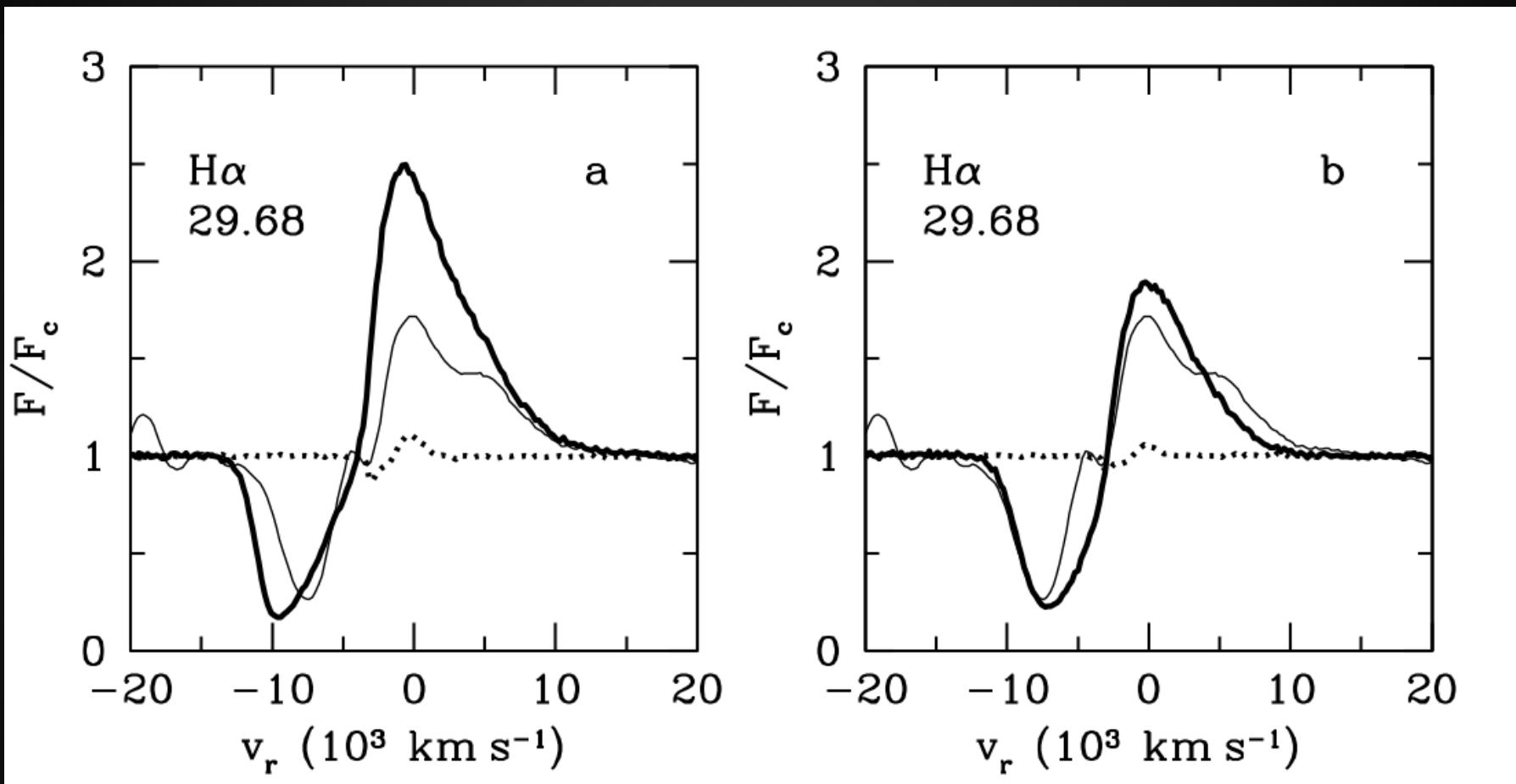
$$\sum_{j \neq i} (n_{z,j} P_{j,i} - n_{z,i} P_{i,j}) = 0$$

# Weak line H- $\alpha$ , SN 1999em, 37 day



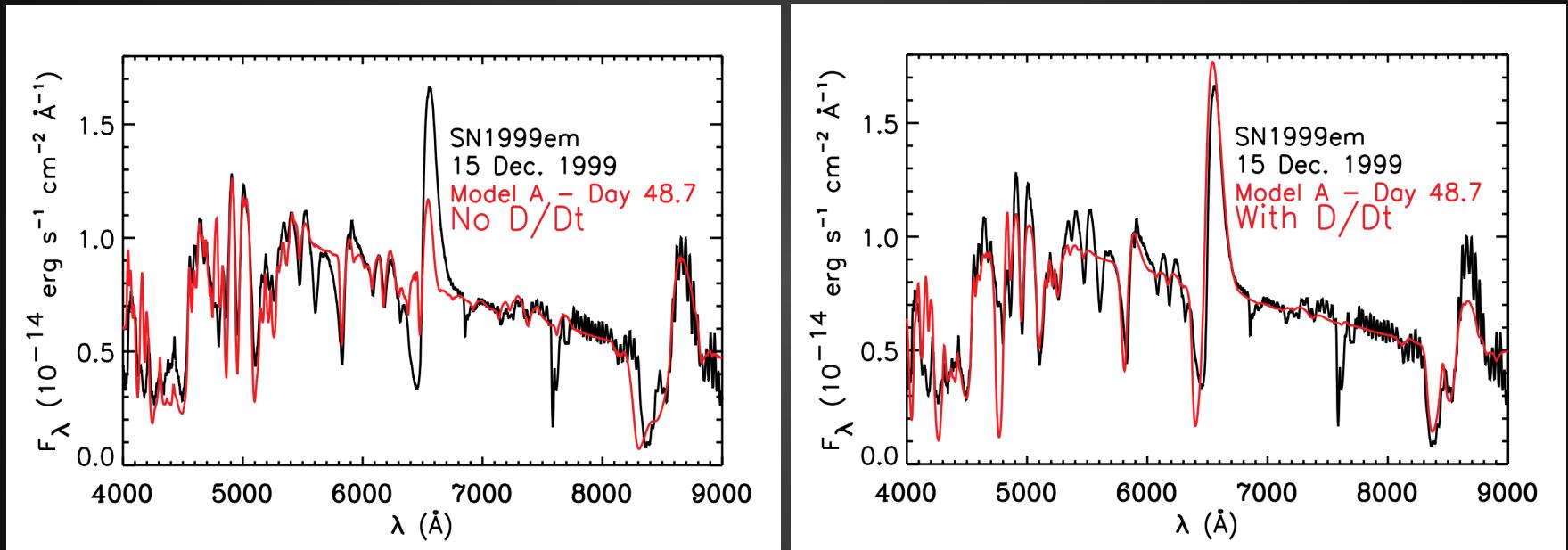
Dessart, L., Hillier, J. 2006, A&A 447, 691–707, CMFGEN

# Time-dependent, SN 1987A, ~30 day



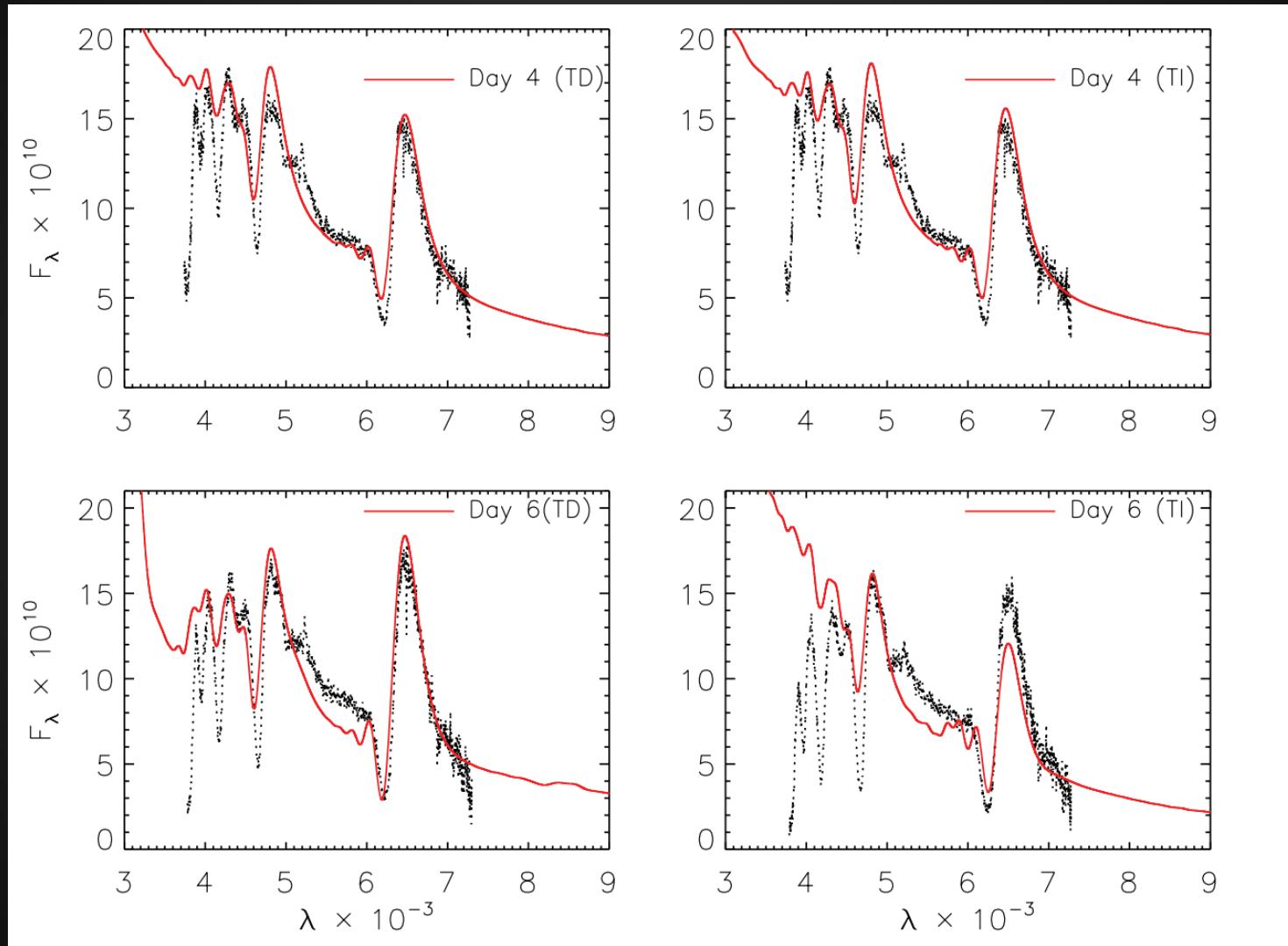
Utrobin, V., Chugai N. **2005**, A&A 441, 271–281

# Time-dependent, SN 1999em, 48 day



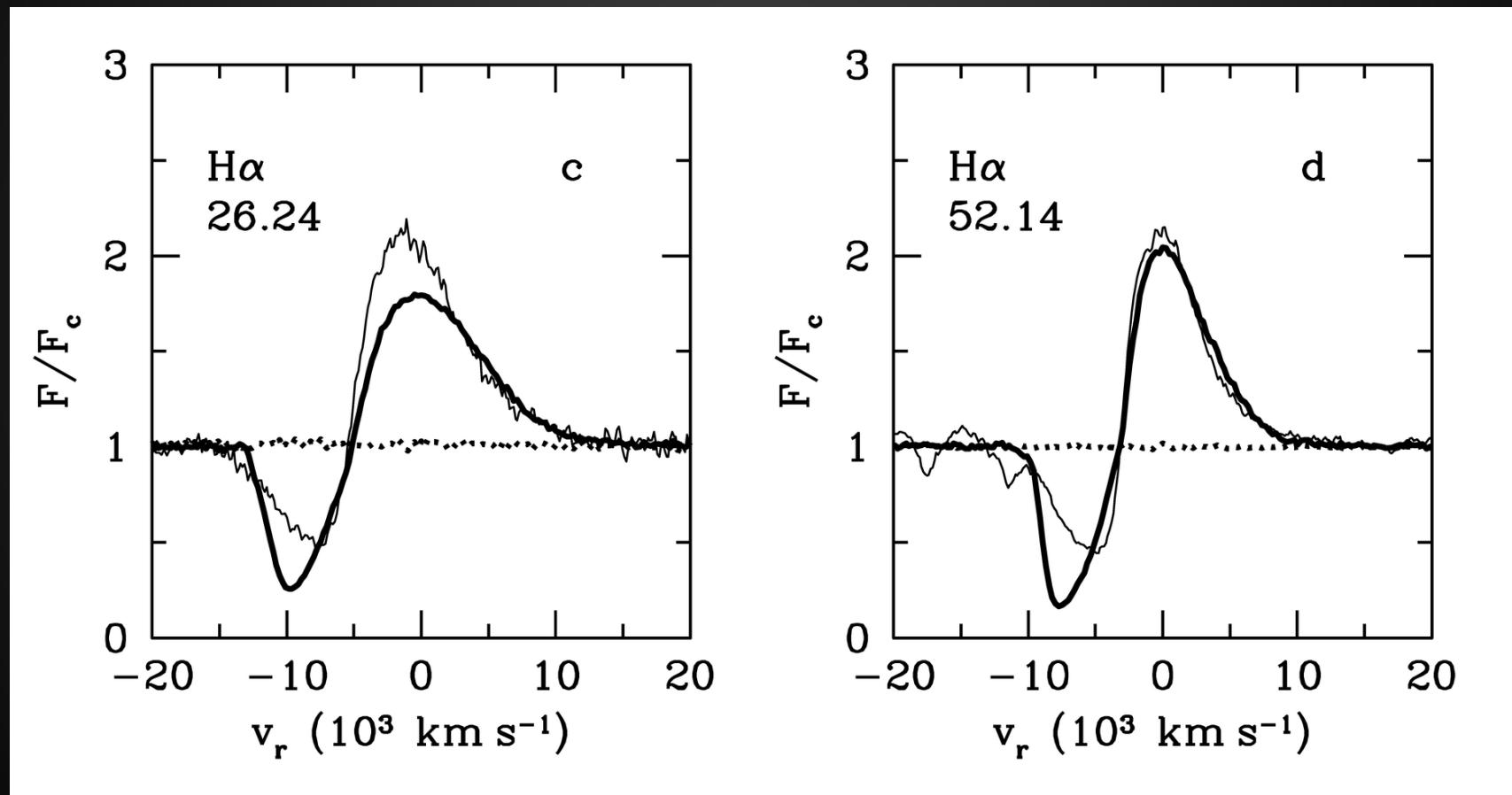
Dessart, L., Hillier, J. 2007, MNRAS 383, 57–74, CMFGEN

# Time-dependent, SN 1987A, 4 and 6 days



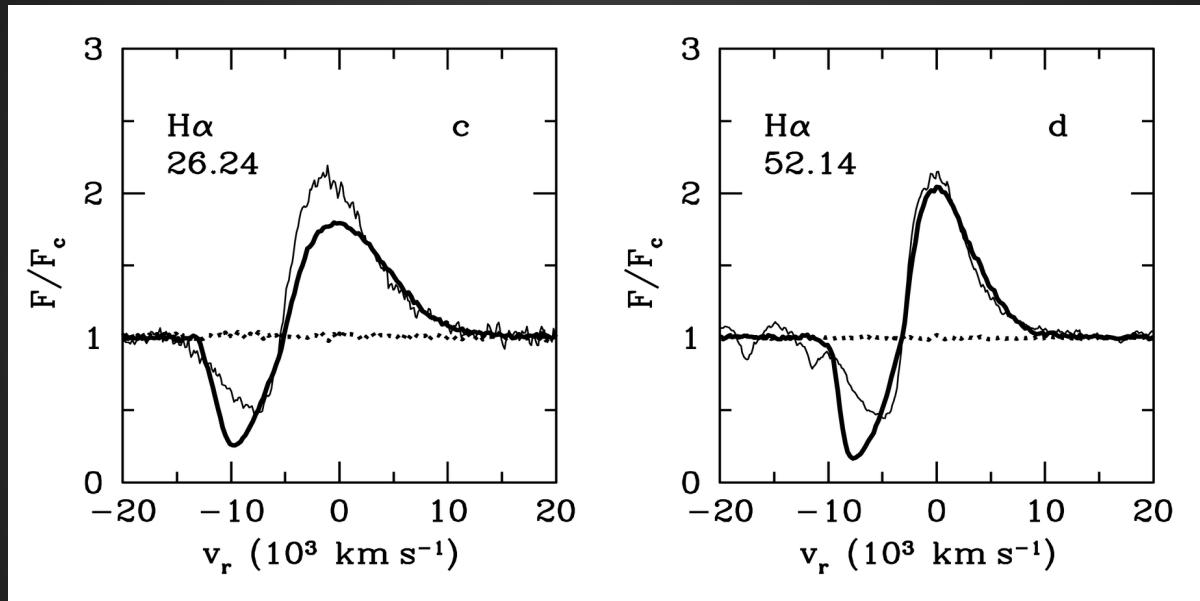
# When the time dependence is important?

SN 1999em, 26 and 52 days



# When the time dependence is important?

SN 1999em, 26 and 52 days



Utrobin, V. P. 2007, A&A 461, 233–251

All the time

# When the time dependence is important?

Time-dependent terms in the statistical- and radiative-equilibrium equations become important a few weeks after explosion (Utrobin & Chugai 2005; Dessart & Hillier 2007a,b).

Dessart, L. et al. 2008, ApJ 675, 644–669

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Dessart, L. et al. 2008, ApJ 675, 644–669

**Few weeks after explosion**

# When the time dependence is important?

SN 1987A also supports the importance of time-dependent rate equations. Therefore, we conclude that time dependence is more important at early times than later times. The effect of multilevel atoms can be seen in Fig. 9 which clearly shows that even at later

De, S., Baron, E. et al. 2010, MNRAS 401, 2081–2092

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De, S., Baron, E. et al. 2010, MNRAS 401, 2081–2092

**At early times**

# Contradiction

Utrobin & Chugai

All the time

Dessart & Hillier

Few weeks after explosion

De & Baron

At early times

# Contradiction



**Break the problem  
into pieces**

# Contradiction



**Break the problem  
into pieces**

**Importance of the  
2 photon decay**

# Contradiction



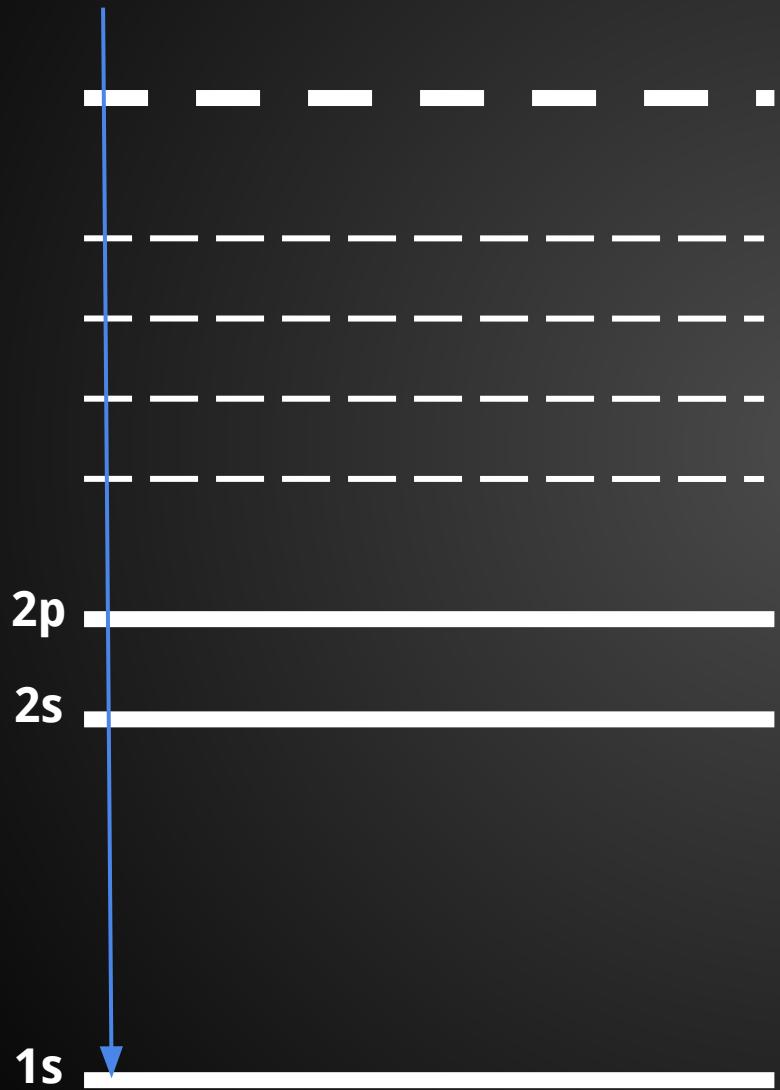
**Break the problem  
into pieces**

**Importance of the  
2 photon decay**

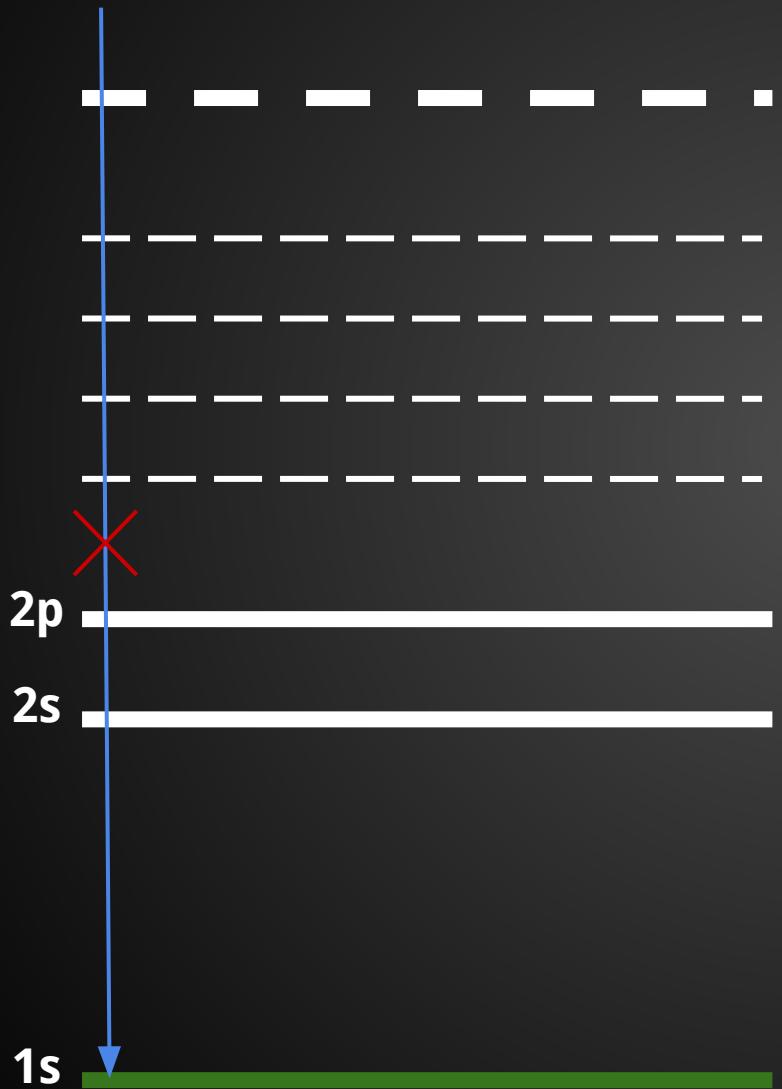
**Importance of the  
I-splitting**

**NO SE among  
I sublevels**

# Where the two-photon process is important?

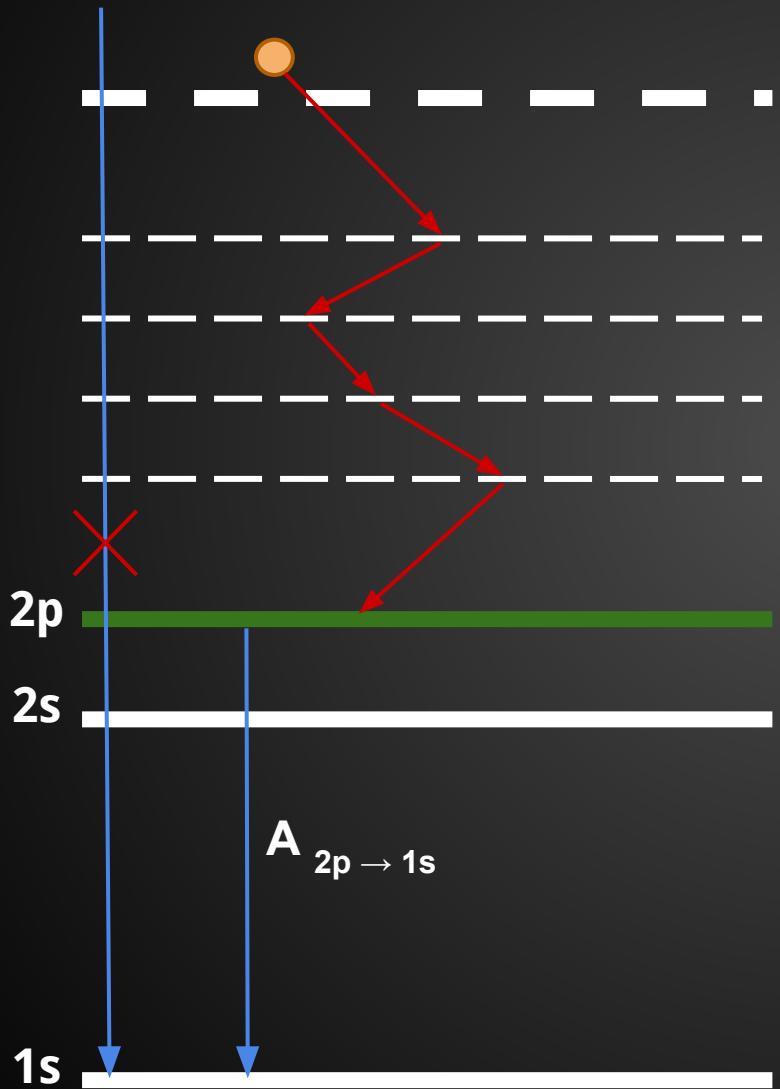


# Hydrogen



Direct recombination  
to the ground state of  
hydrogen is neglected

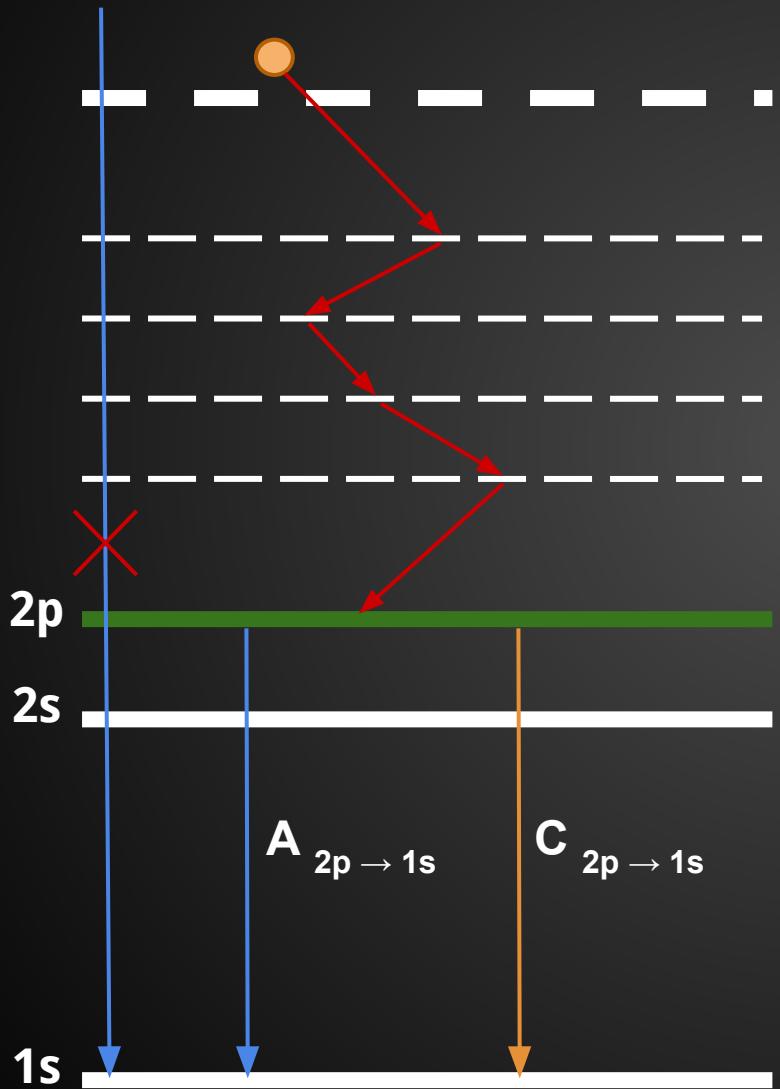
# Hydrogen



Direct recombination  
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Emission  $2p \rightarrow 1s$

# Hydrogen

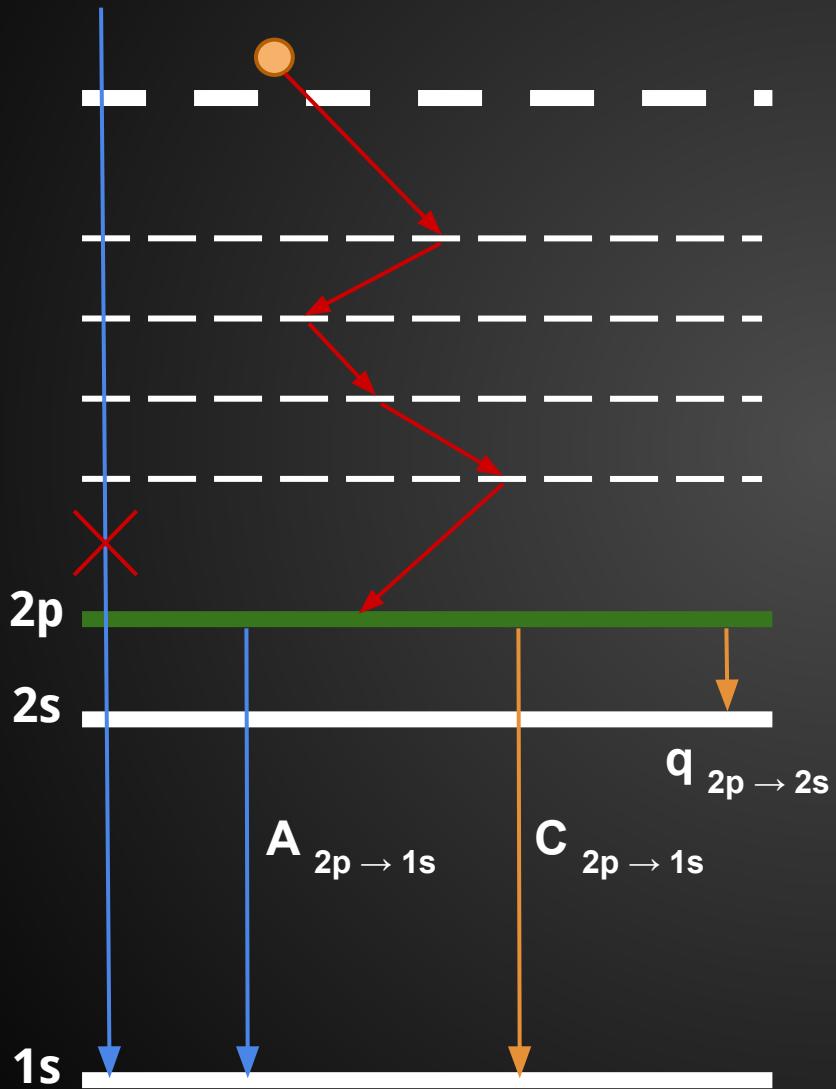


Direct recombination  
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Emission  $2p \rightarrow 1s$

Collisional deexcitation  
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# Hydrogen



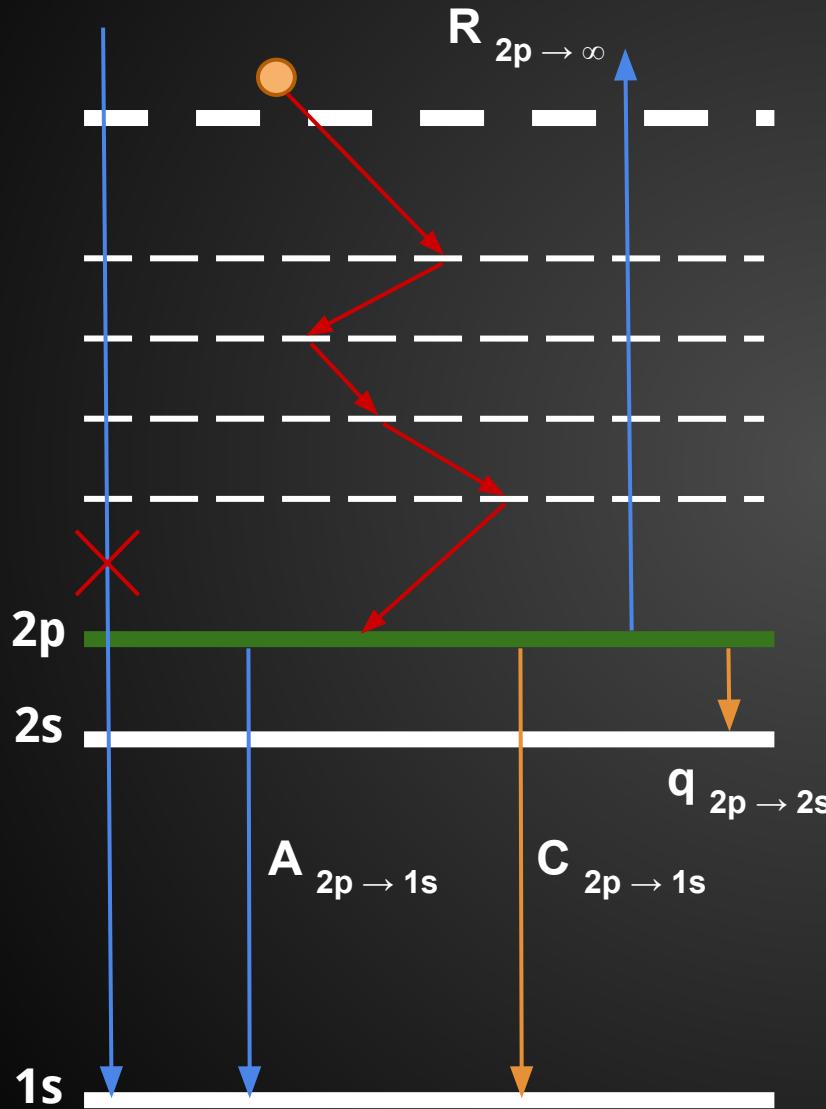
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# Hydrogen



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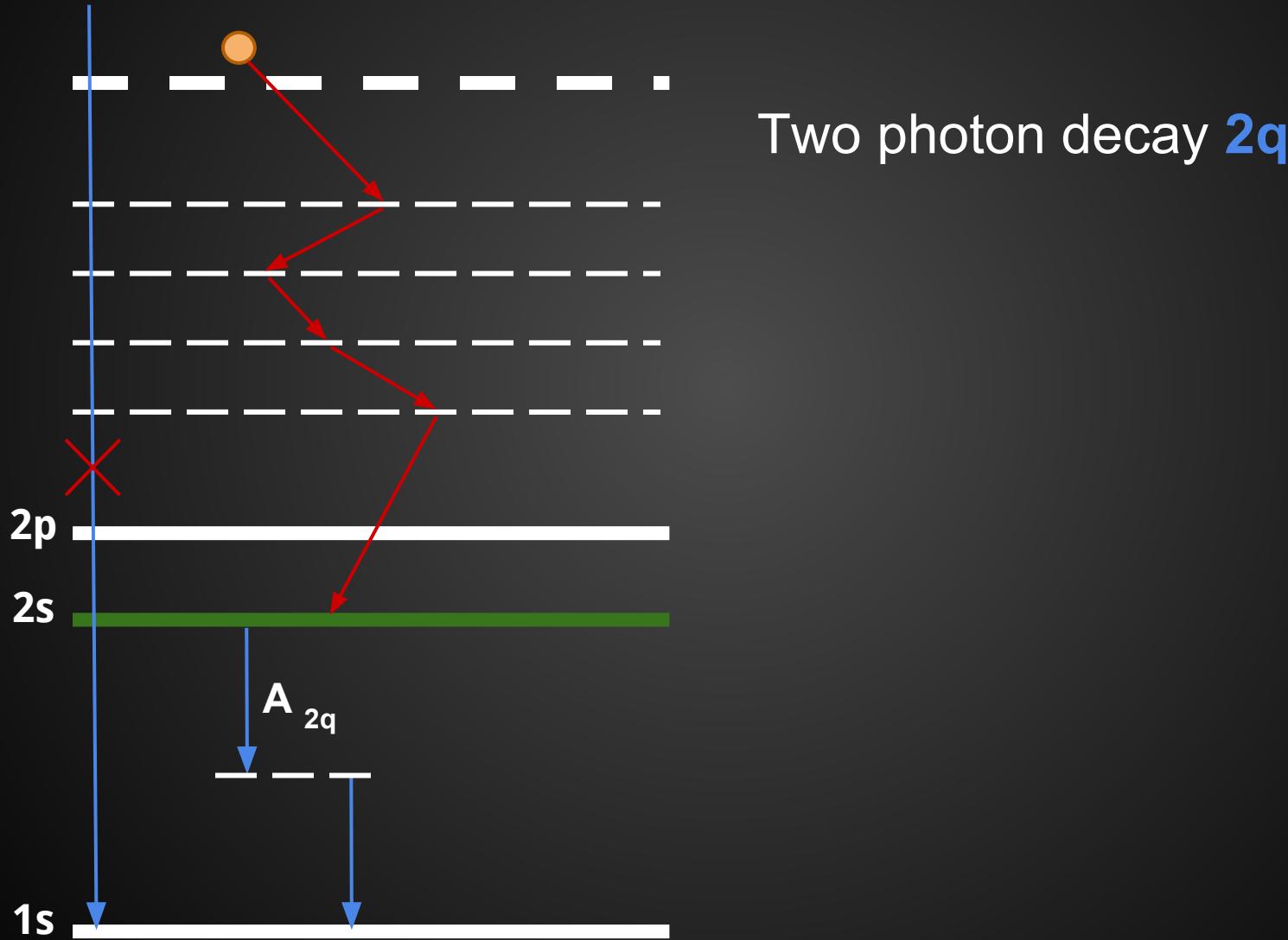
Emission  $2p \rightarrow 1s$

Collisional deexcitation  
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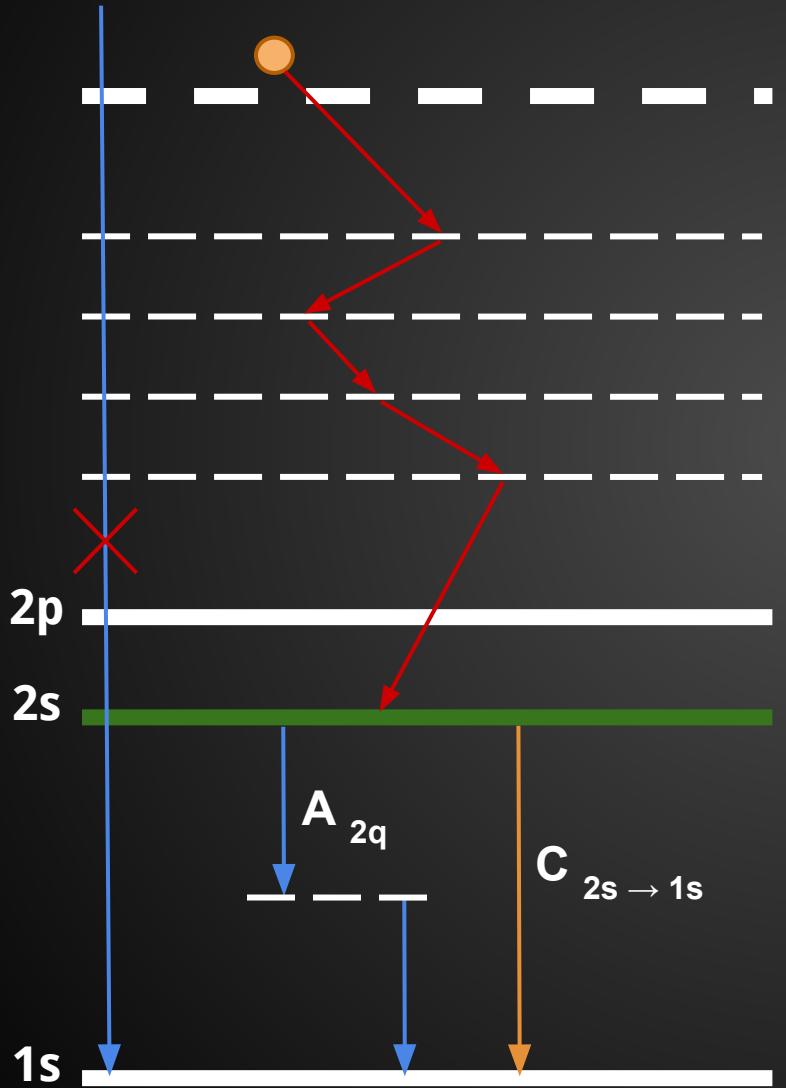
Collisional excitation  
 $2p \rightarrow 2s$

Photoionization  $2p \rightarrow \infty$

# Hydrogen



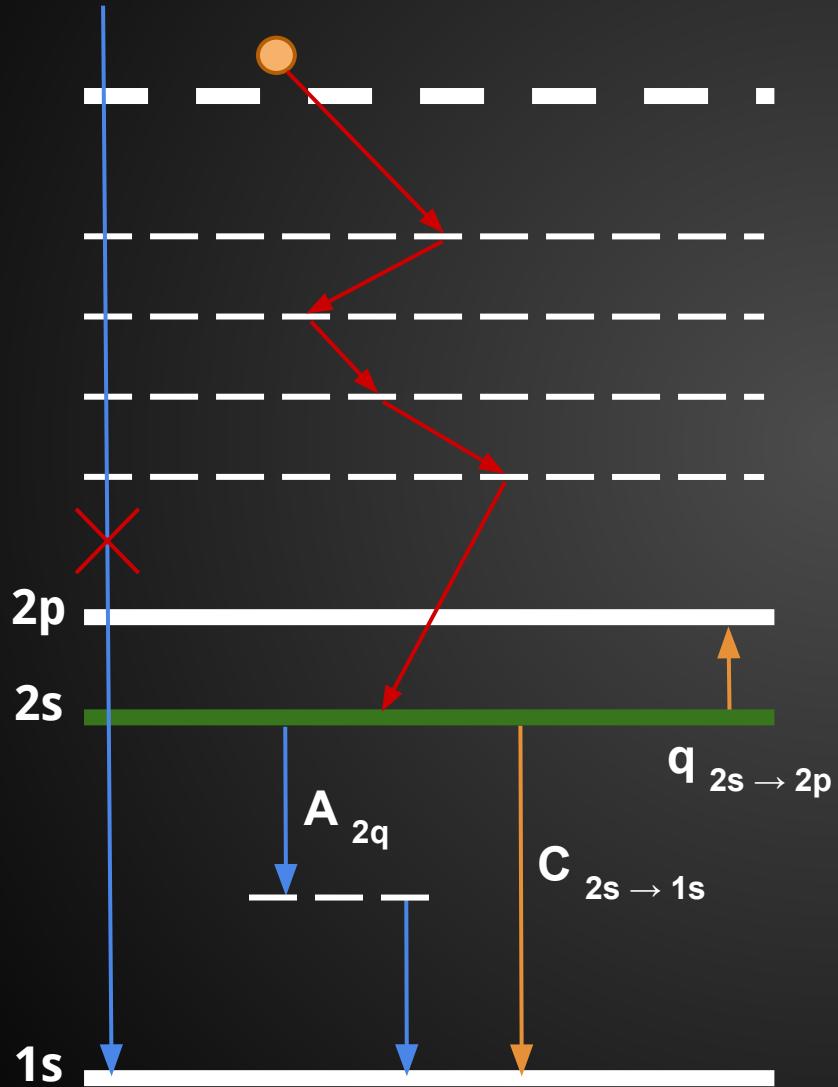
# Hydrogen



Two photon decay **2q**

Collisional deexcitation  
 **$2s \rightarrow 1s$**

# Hydrogen

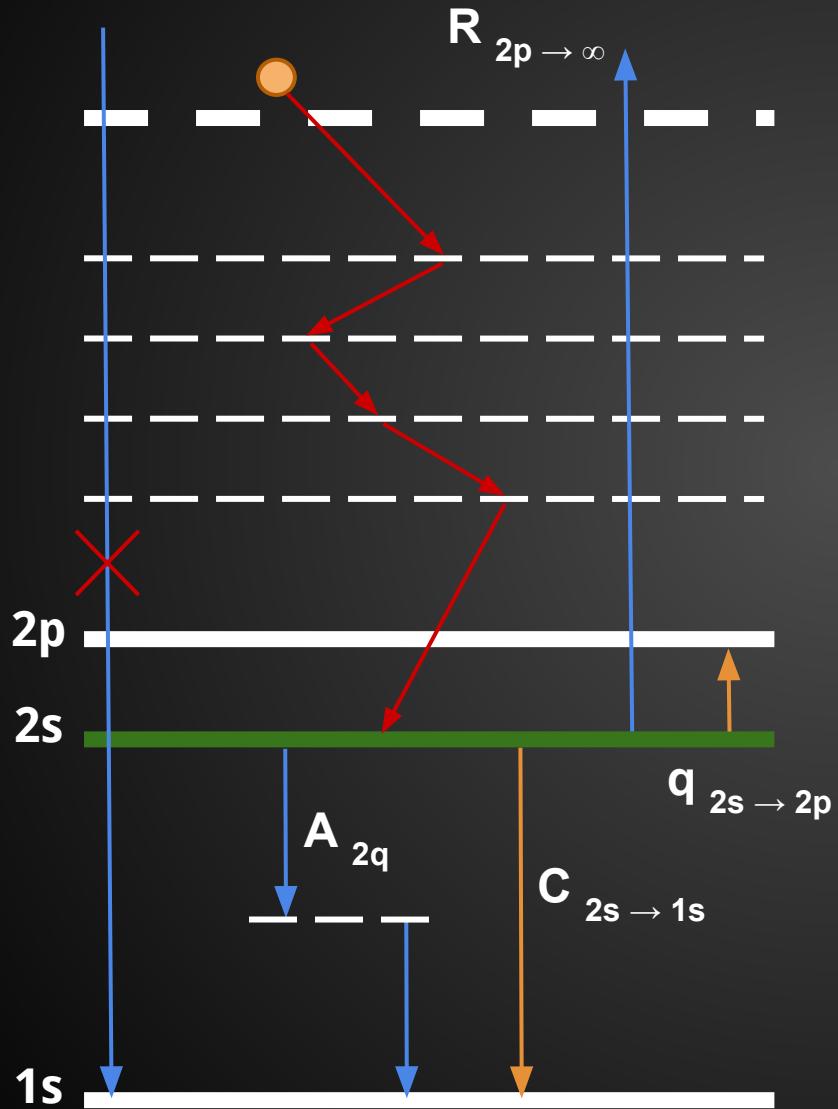


Two photon decay **2q**

Collisional deexcitation  
 **$2s \rightarrow 1s$**

Collisional excitation  
 **$2s \rightarrow 2p$**

# Hydrogen



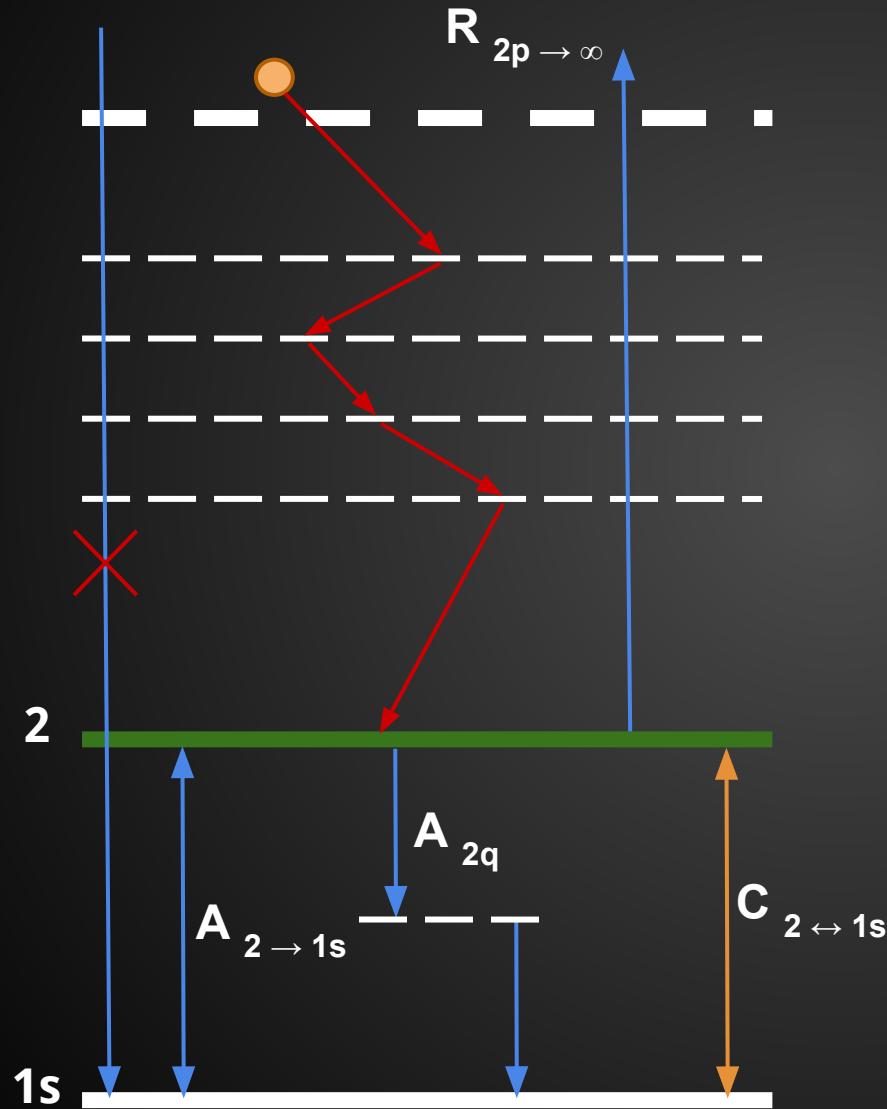
Two photon decay  $2q$

Collisional deexcitation  
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Photoionization  $2s \rightarrow \infty$

# Hydrogen



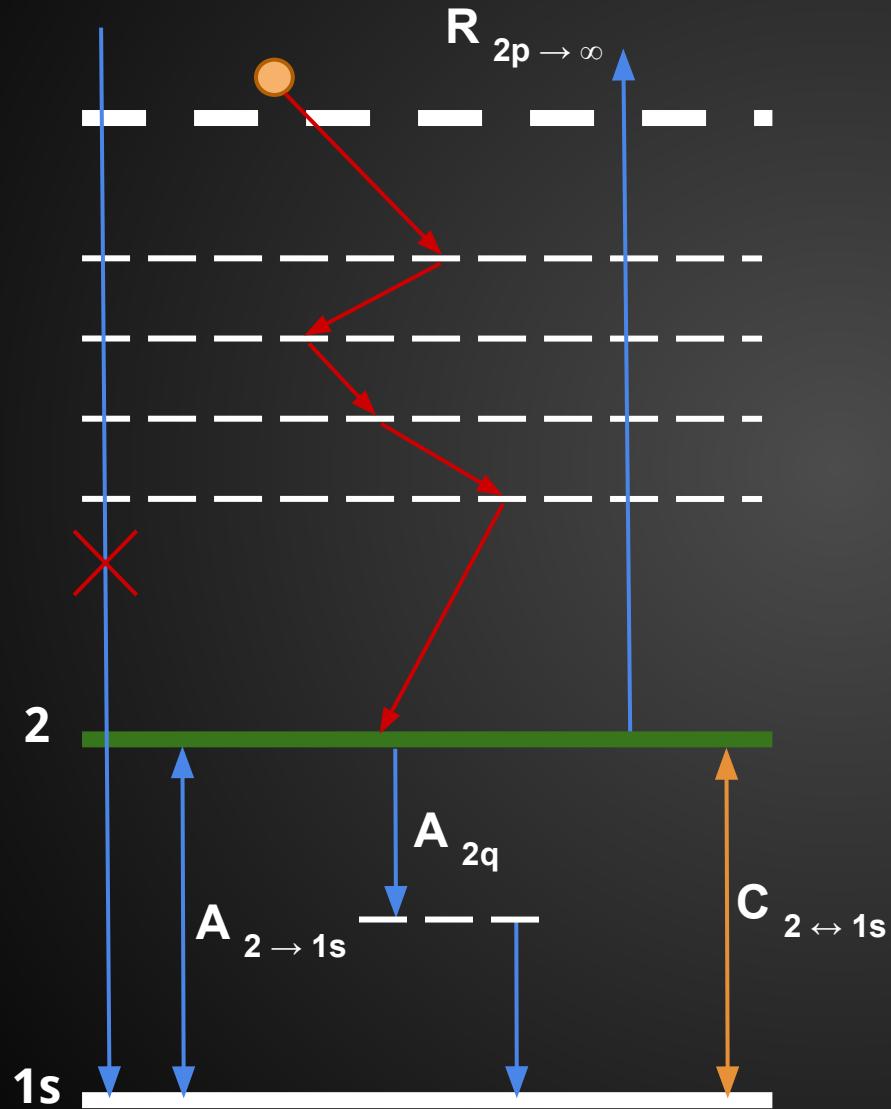
**2s, 2p - LTE  $\Rightarrow$**   
**2 - Super level**

$$n_2 = n_{2s} + n_{2p}$$

$$n_{2s} = \frac{1}{4}n_2$$

$$n_{2p} = \frac{3}{4}n_2$$

# Hydrogen



**2s, 2p - LTE  $\Rightarrow$**   
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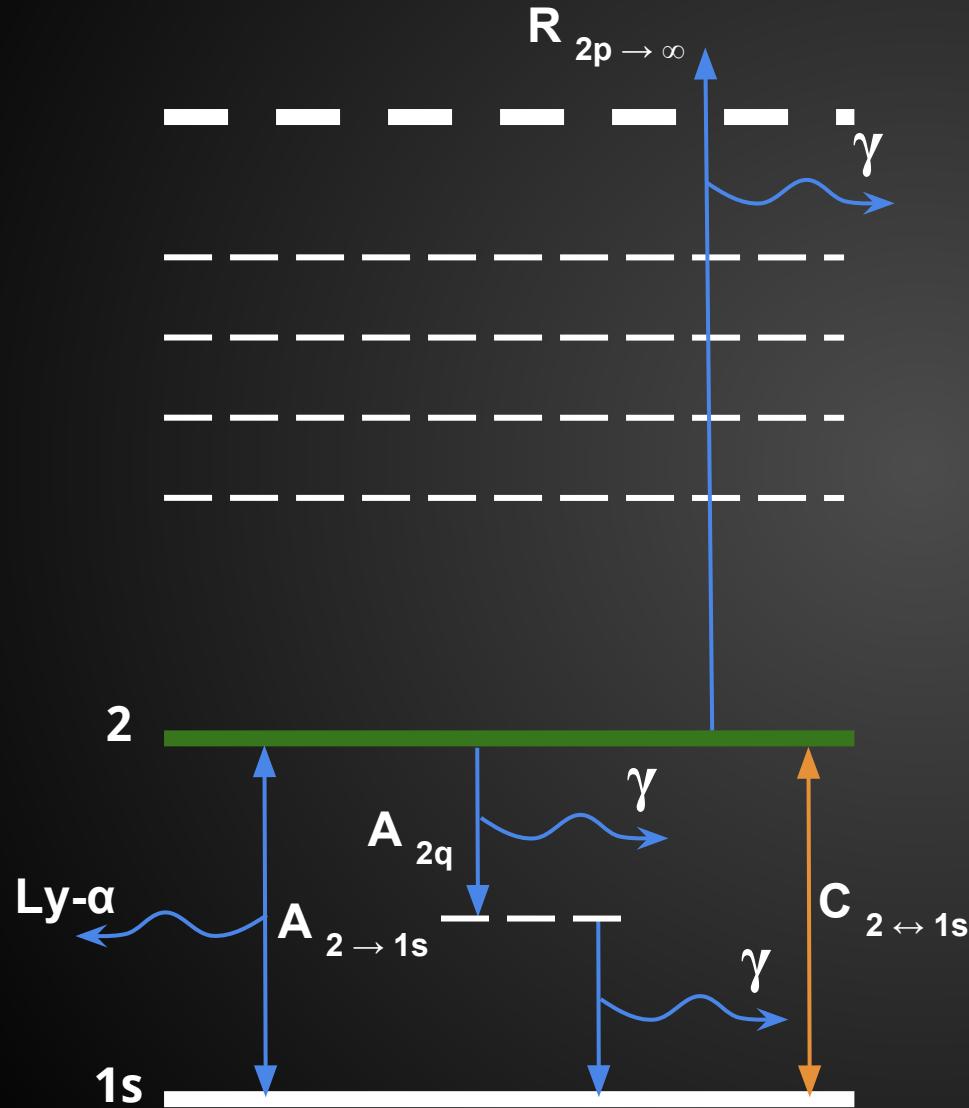
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**SE among l sublevels:  
2s and 2p**

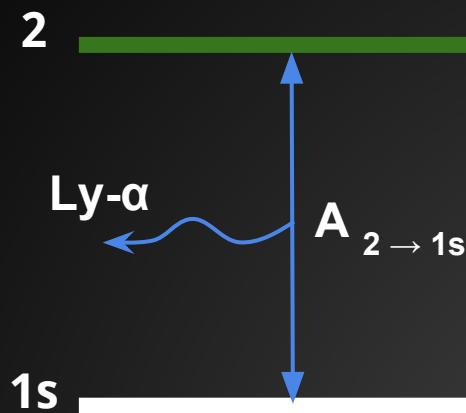
# Hydrogen



**Effectively  
3 states:  
1s,  $n=2$ , e-+p**

Zeldovich et al. 1968,  
Peebles 1968

# Sobolev approximation in Ly- $\alpha$

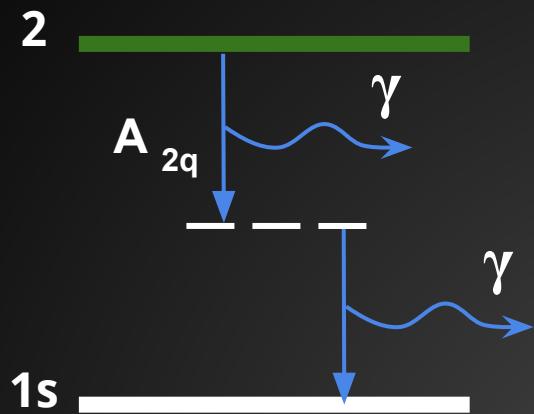


$$P_{\text{esc}} = \beta \sim 1/\tau_S$$

$$P_{\text{esc}} \times A_{2p \rightarrow 1s} \sim \frac{8\pi}{c^3} \nu_{\text{Ly}\alpha} {}^3g_{1s} \frac{1}{g_{2p} n_{1s} t}$$

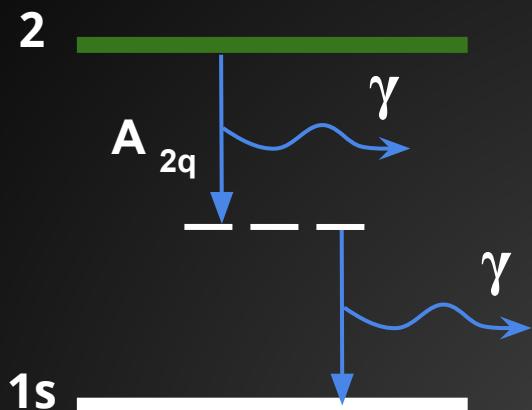
$$\sim 10^{-3} - 10^3 \text{ s}^{-1}$$

Greater in the outer layers



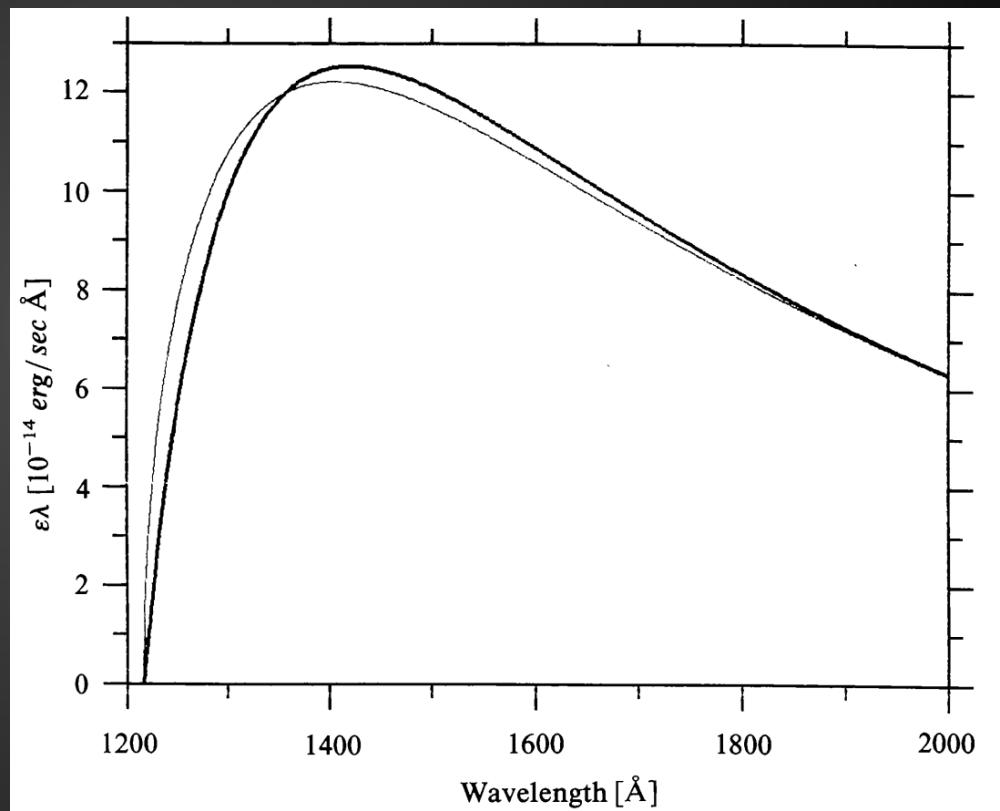
$$A_{2s \rightarrow 1s} \sim 8.225 \text{ s}^{-1}$$

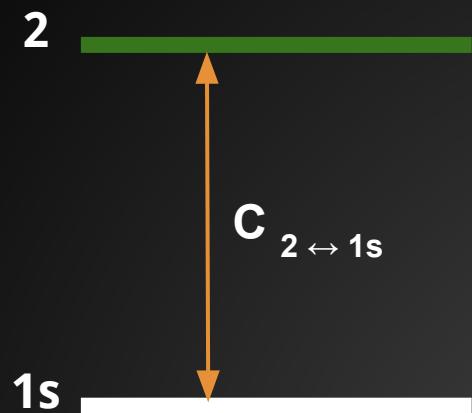
**The same in all layers**



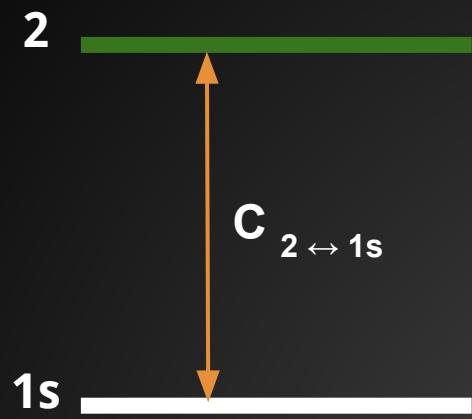
71%  
for frequencies  
higher than  
Balmer jump 3646 Å

$$A_{2s \rightarrow 1s} \sim 8.225 \text{ s}^{-1}$$

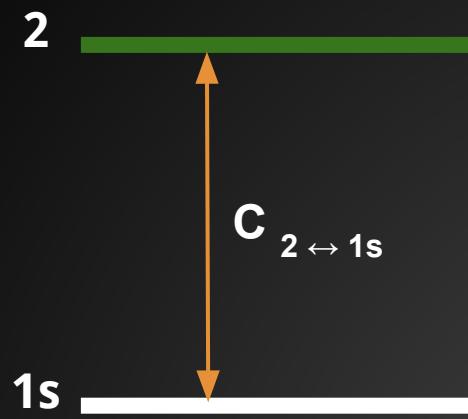




$$n_e n_2 \ C_{2 \rightarrow 1} = \\ = n_e n_2 \ C_{1 \rightarrow 2} \left( \frac{n_1}{n_2} \right)^*$$



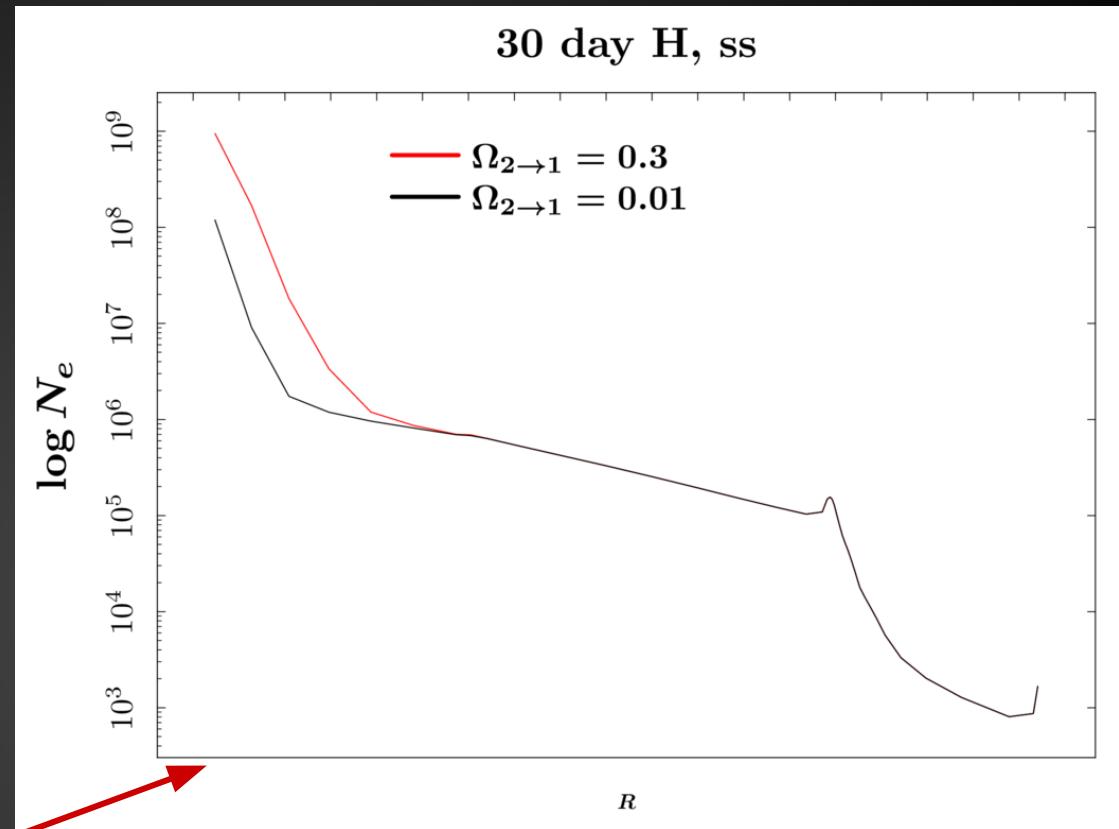
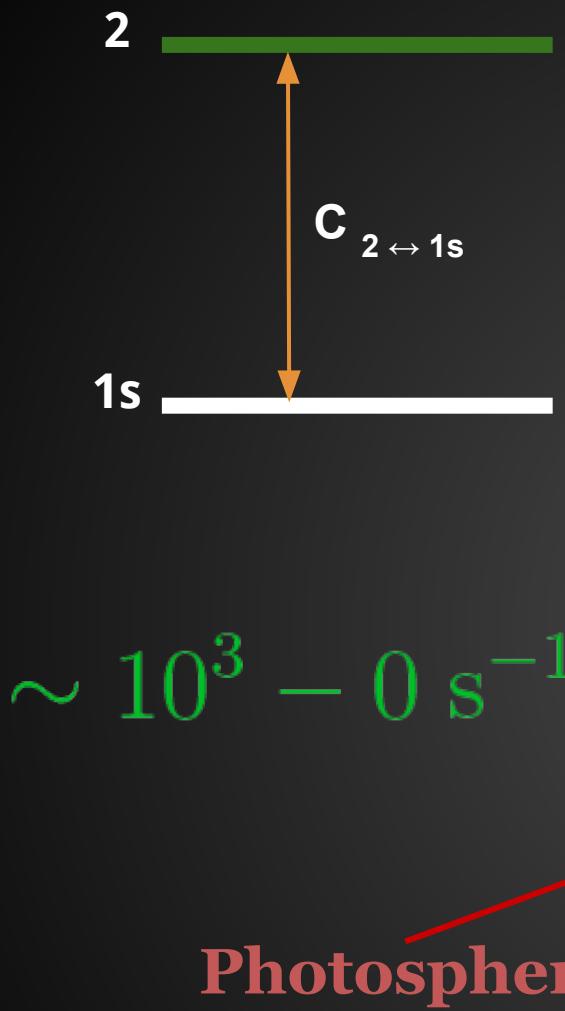
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$$= n_e n_2 \ C_{1 \rightarrow 2} \left( \frac{n_1}{n_2} \right)^*$$
$$n_e n_1 \ C_{1 \rightarrow 2}$$



$$n_e n_2 \ C_{2 \rightarrow 1} = \\ = n_e n_2 \ C_{1 \rightarrow 2} \left( \frac{n_1}{n_2} \right)^*$$

A series of mathematical expressions connected by arrows. A red downward arrow points from the first expression to the second. A red upward arrow points from the second expression to the third. The first expression is  $n_e n_2 \ C_{2 \rightarrow 1}$ . The second expression is  $= n_e n_2 \ C_{1 \rightarrow 2} \left( \frac{n_1}{n_2} \right)^*$ .

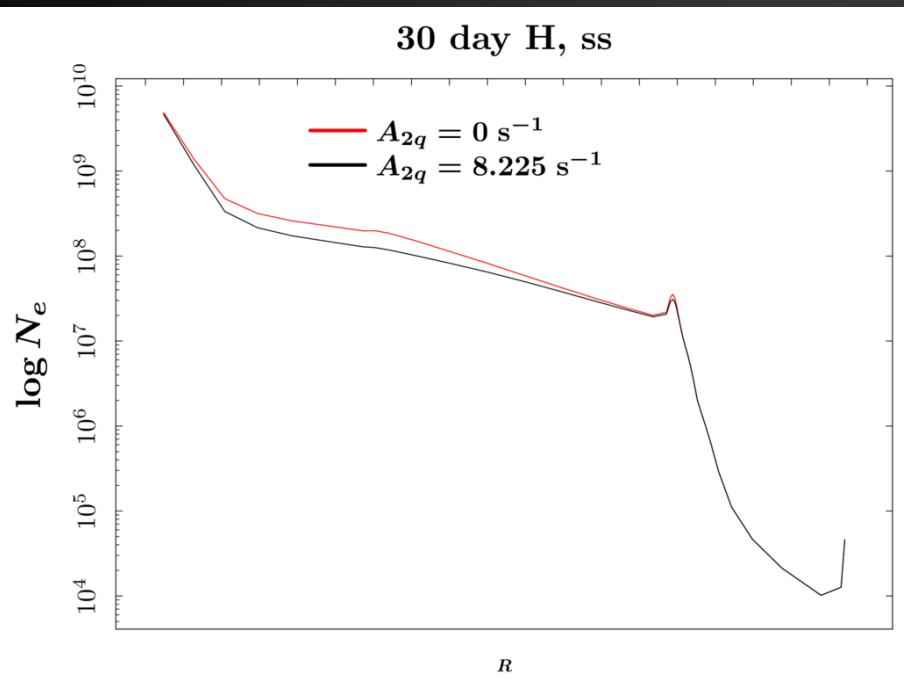
$$n_e \ C_{1 \rightarrow 2} \left( \left( \frac{n_1}{n_2} \right)^* - \frac{n_1}{n_2} \right)$$



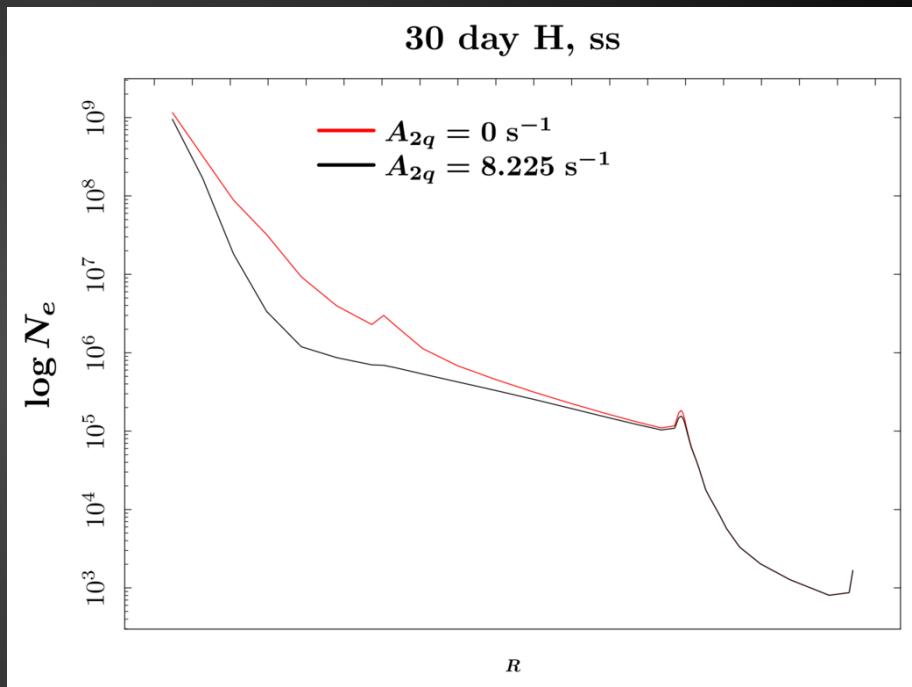
Greater in the **near-photospheric layers**

# Hydrogen star, 2 level + continuum

30 day



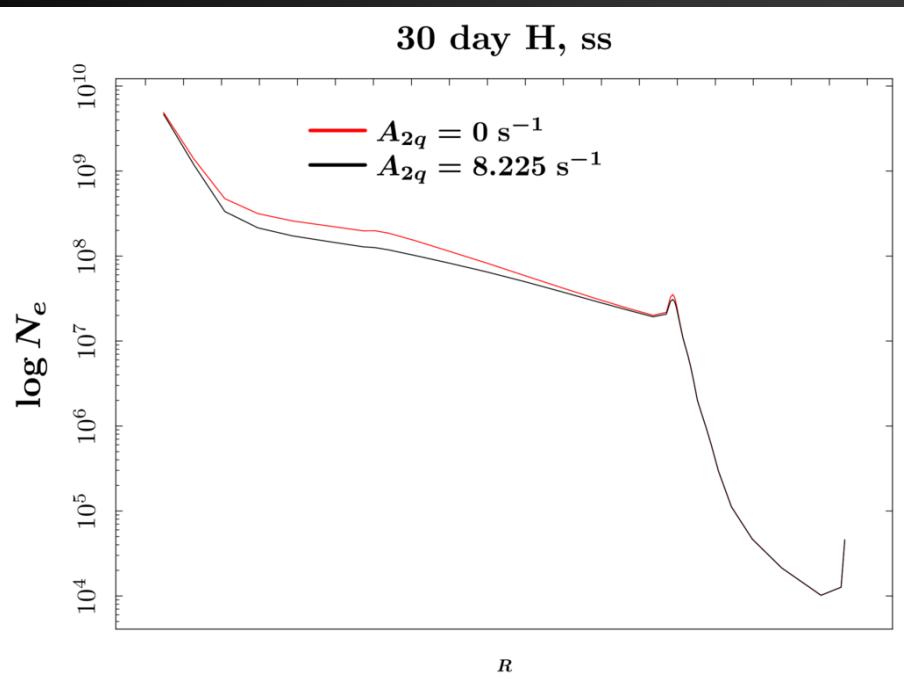
Model A



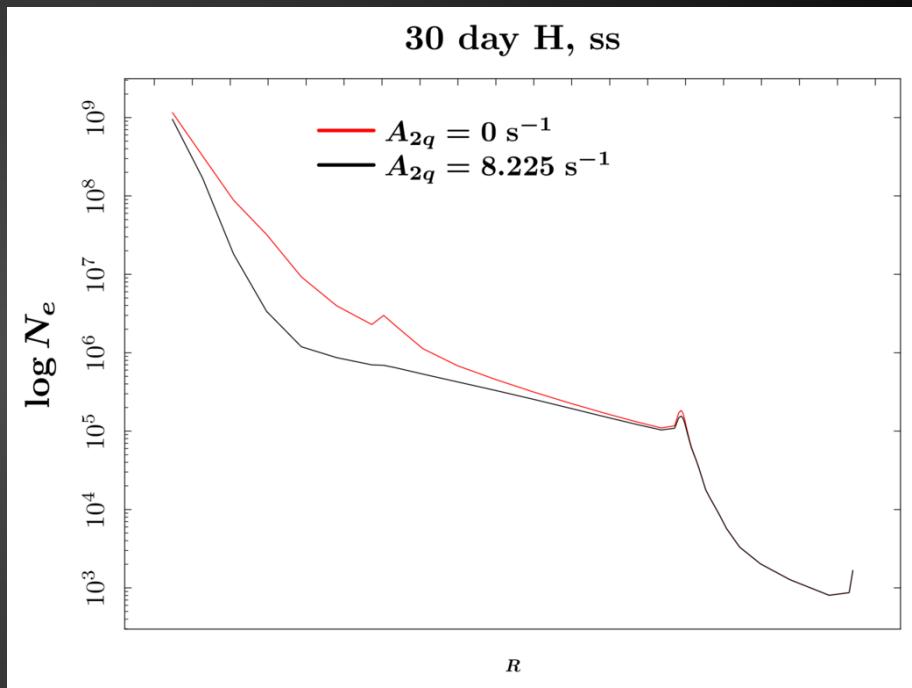
Model B

# Hydrogen star, 2 level + continuum

30 day



Model A



Model B

Important in the middle layers

# Where the two-photon process is important?

quite different when compared to models C and D. Table 2 shows the changes due to the  $2\gamma$  process. For model A, at low optical depths ( $\tau_{\text{std}} \sim 10^{-4}$ ) turning on the  $2\gamma$  process produces about a 20 per cent change in the free electron density, but for  $\tau_{\text{std}} \gtrsim 10^{-3}$  no significant change is seen. For model B, there is a significant reduction in the free electron density due to the inclusion of the  $2\gamma$ .

De, S., Baron, E. et al. 2010, MNRAS 407, 658–668

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4-level  
1s, 2s, 2p<sub>1/2</sub>, 2p<sub>3/2</sub>

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4-level  
1s, 2s, 2p<sub>1/2</sub>, 2p<sub>3/2</sub>

Important in the **outer layers**  
for pure hydrogen models

# The Flexible Atomic Code (FAC)

Ming Feng Gu



Hydrogen star, 81 level + continuum

If there is no collision process the  
effect disappears!

# **Further steps (instead of conclusions)**

- The time dependence effect is not fully understood
- We need to reject Sobolev approximation in Ly $\alpha$  decays
- We need to include b-b and b-f collisions
- Metal-rich models